|  |  |
| --- | --- |
|  |  |

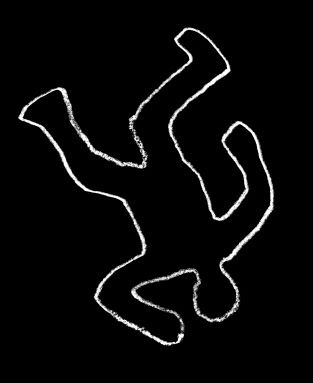
Tab 1

**Background**

**The Ebola Epidemic**

The Western African Ebola virus epidemic (2013–2016) was the most widespread outbreak of Ebola virus disease in history, causing major loss of life and socioeconomic disruption in the region. The first cases were recorded in Guinea in December 2013; later, the disease spread to neighboring Liberia and Sierra Leone, with minor outbreaks occurring elsewhere.[1]

**Patient Zero**

Just as the World Health Organization (WHO) and local health organizations began to think that the epidemic was over, policeman in Monrovia (Liberia) found a body of a man in an abandoned warehouse. The autopsy shed light on several important facts:

* **The man was stabbed 18 times.**
* **The man was a member of a local gang.**
* **The man had been infected with Ebola.**

Let's call this man **“patient zero”.**

**Contact Tracing**

The next step is to trace the spread of Ebola starting from patient zero. We need *a design or model* that would help us visualize patient zero, everyone he has been in contact with, and the connections between these people (who has been in contact with whom).

Think for a moment—**how can we do this?**

***Brainstorming space:*** ***Answers will vary. This space is just to get students***

***thinking about the problem, so all answers are valid as long as students try.****\_\_\_*

\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

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**Welcome to Graphs!**

**What are graphs?**

**Graphs are mathematical structures used to study pairwise relationships between objects.**

Check out [this link](http://www.martingrandjean.ch/wp-content/uploads/2016/05/airports-map-small.png)[[1]](#footnote-1)[2] to see an example of how we can represent airline traffic as a graph. Airports are represented by circles of various sizes. In a graph, these circles are called **"nodes" (or vertices)**. The flights themselves are lines that connect the nodes together. These lines are called **"edges"**.

As you see, a graph is essentially a pair of *two* collections of data or sets. One of these sets contains all the **nodes (or vertices)**, and the second set contains all the **edges**.

*e.g.*

|  |  |
| --- | --- |
| **Set 1: Nodes or Vertices (V)**  **Airports** | |
| **Node #1** | Background pattern  Description automatically generatedJohn F. Kennedy Int. Airport (New York, ) |
| **Node #2** | Galeão Int. Airport (Rio de Janeiro, ) |
| **Node #3** | Madrid-Barajas Airport (Madrid, ) |
| **Node #4** | O. R. Tambo Int. Airport (Kempton Park, ) |
| **Node #5** | Suvarnabhumi Airport (Bangkok, ) |

|  |  |
| --- | --- |
| **Set 2: Edges (E)**  **Flights** | |
| **Flight #1** | JFK ----- Galeão |
| **Flight #2** | JFK ----- Madrid-Barajas |
| **Flight #3** | JFK ----- O. R. Tambo |
| **Flight #4** | Madrid-Barajas ----- Galeão |
| **Flight #5** | Madrid-Barajas ------ O. R. Tambo |
| **Flight #6** | O. R. Tambo ----- Suvarnabhumi |

**We can mathematically represent a graph (G) as:**

**G = (V,E).**

*Where:*

* *V* is the set of vertices, and,
* *E* is a set of edges.

E is made up of pairs of elements from V (unordered pair).

In our previous example, *V* would represent all airports, and *E* would represent flights between pairs of airports.

**Let's get back to the Ebola problem**

We will create a graph where:

* Nodes will represent people who were unfortunate enough to be in contact with patient zero, and,
* Edges will represent how these people relate to each other (how or why did they come to be in contact with patient zero and with each other).

**TEACHERS**

The nodes and edges that students need to add to the following graphs are marked in blue ink.

Let's start by adding our Patient Zero to the graph. Because he was a member of a gang, and because he is patient *zero,* we will refer to him as “G0” from now on:

Chart, bubble chart

Description automatically generated

**Body Discovery**

The body was discovered by three police officers. Let’s add them to the graph and label them as P1, P2, and P3:

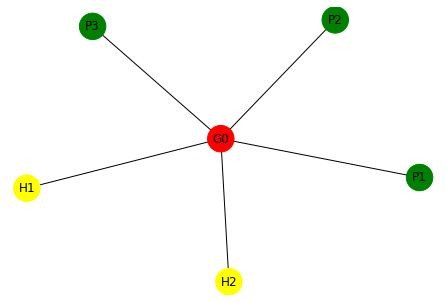
A picture containing skiing, green

Description automatically generated

**First Healthcare Responders**

We also know from the police reports that *two* emergency medical technicians (EMT) had responded to the scene. These EMTs performed the initial examination, pronounced G0 dead, and removed the body from the scene.

*Your turn* to add the healthcare workers to the graph. Label the nodes that represent healthcare workers as “H1” and “H2”:



**More Connections**

Police officers and first responders interacted with each other at the crime scene, so they could have potentially spread the infection to each other. So at the very least, let's connect all responders who were at the scene:

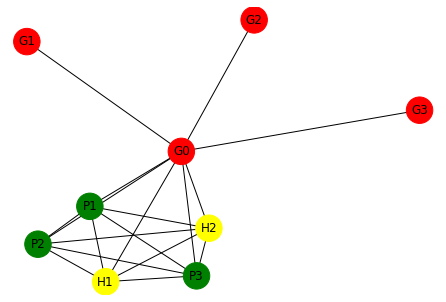
A picture containing accessory, green

Description automatically generated

**Dang—we have to think about other gang members**

Through witness reports, the police have determined that the murder was committed by three other gang members, all of whom participated in the stubbing and thus were exposed to G0's blood. We need to add them to the graph.

*Your turn*. Use the labels “G1”, “G2”, and “G3” to add them to the graph:



**Getting the body to the morgue**

When G0's body was transported to the morgue, *four* more people came into contact with it—a coroner who performed the autopsy (“H3”), the coroner's assistant (“H4”), and two morgue workers who moved the body (“H5” and “H6”). Additionally, the two workers who moved the body (H5 and H6) came in contact with the first EMT (“H1”) while signing the transfer paperwork.

We have already added H1’s edges to H5 and H6. *Your turn* to add the remaining nodes and edges:

*Hint: This graph is missing two nodes and four edges.*

A picture containing polygon

Description automatically generated

**Family is important**

Further police investigation showed that some of the police officers, healthcare workers, and even gang members had family members. We'll prefix family member nodes with the letter "F":

Diagram

Description automatically generated with low confidence

**A sordid twist to the story**

After interviewing family members and friends of some of the gang members, the police found that one of the gang members, G3, frequented a brothel... so now we have to track brothel workers with whom G3 might have had contact. Let's label brothel workers nodes with 'B':

A picture containing diagram

Description automatically generated

This is the song that never ends...

As it turned out, some of the sex workers also had families, and other clients, and friends, and other people that they interacted with. Police officers who were on the scene interacted with their coworkers. The Ebola virus will keep spreading, and the graph will keep growing.

**The Problem**

After successfully contact-tracing and alerting people of a possible epidemic, scientists are gathering more data to predict how fast the virus will spread, and Dr. Wilkinson needs your help.

Dr. Wilkinson wants to find out how many people will be infected on the **7th** day of the epidemic. From other sources, you have been told that, **on average, one sick person infects from one to two other people**[3]. **Let’s say two**, for this exercise. You have been told that there’s a formula—the formula for Exponential Growth—that can help predict how many people will be infected at a certain point:

***Formula for Exponential Growth***

x(t) = x0 \* bt

*in which:*

* *x(t)* is the number of cases at any given time *t.*
* *x0* is the number of cases at the beginning of the epidemic.
* *b* is the number of other people that one sick person infects.

What are the steps that *Dr. Wilkinson* needs to take to find the solution?

**The Solution**

Let’s list ***all[[2]](#footnote-2)*** the steps Dr. Wilkinson needs to take:

**TEACHERS**

Explain the limitations of the Exponential Growth formula. (e.g. That it only fits the initial phase of an epidemic, etc.)

**Plain English**

***Fill in the Blanks***

**1.** Well, Dr. Wilkinson first needs you to tell her the value of the variables, of course. Because she assumes that there was *one* initial case (that is, that x0 = 1), she will not ask you about the value of x0—that’s an easy one. But she will certainly ask you about the next variable: “Okay, so tell me, on average, how many other people does one sick \_\_\_\_\_\_**person infect**\_\_\_\_\_\_?”

**2.** And you answer: “\_**2**\_”. *(Hint: We gave you this number on the previous page.)*

**3.** Then she needs to calculate: x(7) = \_\_**1**\_\_ \* \_\_**27**\_\_ = \_\_**128**\_\_.

**4.** Finally, she concludes, “There will be \_\_**128**\_\_\_ infected people on the day # \_\_**7**\_\_ of the epidemic.”

**Generalized Solution**

Dr. Wilkinson now wants you to code a program that will allow her to calculate how many people will be infected at *any* day of the outbreak of *any* virus.

Think for a moment: **What would the program need to know to do this? And what actions would it need to do?** Use the brainstorm space below to answer these questions.

*Note: It will be assumed that there was one initial case, so we can just forget about that variable and use the simplified formula: x(t) = bt .*

***Brainstorming space:*** ***Answers will vary. This space is just to get students***

***thinking about the problem, so all answers are valid as long as students try.****\_\_\_*

\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

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Well, the program should:

* Ask the user how many other people one sick person infects.
* Ask the user the day of the epidemic for which it should calculate.
* Calculate and let users know the result of the calculation.

We will list all the steps in detail in the next exercise, but for now, let’s introduce you to pseudocode and variables.

**Pseudocode**

Let’s start translating our solution into a language that is *similar* to the languages that computers understand. On the limbo between plain English and programming languages, there is pseudocode. For the next exercise, we will use a variation of the conventional pseudocode.

**Variables**

Computers cannot “remember” the user’s input unless you *store* this information somewhere. To do this in programming, we use variables.

A picture containing text, table

Description automatically generatedA glass of beer

Description automatically generated with low confidenceYou can think of variables as containers. Like a regular container, the content you put inside a variable can *vary* (thus its name!) depending on what you want it to store. And like a tag on a regular container, it is wise to give variables a distinct name that alludes to what the variable is storing (e.g. “x(t)”). Unlike a regular container, however, spaces between words and parenthesis are normally not allowed. **Thus, “x(t)” may be better expressed as “xt”.**

**Matching Pairs Game + Fill in the Blanks**

Match each action of the generalized solution in plain English (left gray column) with its pseudocode translation (right gray column). Use the options on the green chart to fill in all the blanks.

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| Choose from the following options to fill in the blanks: | | | | | | |
|  |  |  |  |  |  |  |
| does one sick person infect |  | exponent\_result |  | X21 |  | For what day of the epidemic do you want to calculate? |
|  |  |  |  |  |  |  |
| b |  | xt |  | answer |  | B2 |
|  |  |  |  |  |  |  |
| P1 |  | G4 |  | x0 |  | t |

***Note: Some of these options will not be used, and some may be used more than once.***

*Tip: If possible, keep the color-coding of the options on the green chart (e.g. “answer” is turquoise; “xt” is orange.)*

|  |  |  |
| --- | --- | --- |
| **Step-by-Step**  **Generalized Solution For Coding** |  | **Pseudocode** |
| **1.** Ask: “On average, how many other people \_\_**does one sick person infect**\_\_?” |  | POWER \_\_**b**\_\_ ^ \_\_**t**\_\_ |
| **2.** When the user answers, save this answer in a variable called “\_**b**\_”. |  | ASK On average, how many other people \_**does one sick person infect**\_? |
| **3.** Ask: “**For what day of the epidemic do you want to calculate**?” |  | ASK **For what day of the epidemic do you want to calculate**? |
| **4.** When the user answers, save this answer in a variable called “\_**t**\_”. |  | SAY There will be \_\_**xt**\_\_ infected people on the day # \_\_**t**\_\_ of the epidemic. |
| **5.** Calculate: \_\_**b**\_\_ ^ \_\_**t**\_\_ |  | SET xt TO exponent\_result |
| **6.** … and save the ***result*** of the calculation in a variable called “**xt**”. |  | SET b TO \_\_answer\_\_ |
| **7.** Communicate to the user: There will be \_\_**xt**\_\_ infected people on the day # \_\_**t**\_\_ of the epidemic. |  | SET t TO \_\_answer\_\_ |

***Reorder the Pseudocode***

Now that you have matched each step with its pseudocode translation, write the whole pseudocode below in the right order.

*Remember to write each step in a different line. If possible, keep the color-coding of the pseudocode lines above. (E.g. “ASK” is turquoise; “SET” is orange.)*

**TEACHERS**

It is okay if students cannot keep the color-coding of the given words/phrases/symbols (e.g. they may not have color pencils at hand, or they may be filling out the worksheet digitally). However, when working on the Scratch part (next section), make them refer to the next previous to check what color each word/phrase/symbol is supposed to be. *(“answer” is turquoise; “xt” is orange, etc.)*

ASK On average, how many other people does one sick person infect?

SET b TO answer

ASK For what day of the epidemic do you want to calculate?

SET t TO answer

POWER b ^ t

SET xt TO exponent\_result

SAY There will be xt infected people on the day # t of the epidemic.

**TEACHERS**

**Revise the students’ pseudocode. It is important that they have it right before they start coding on Scratch.**

Tab 2

**Getting Started**

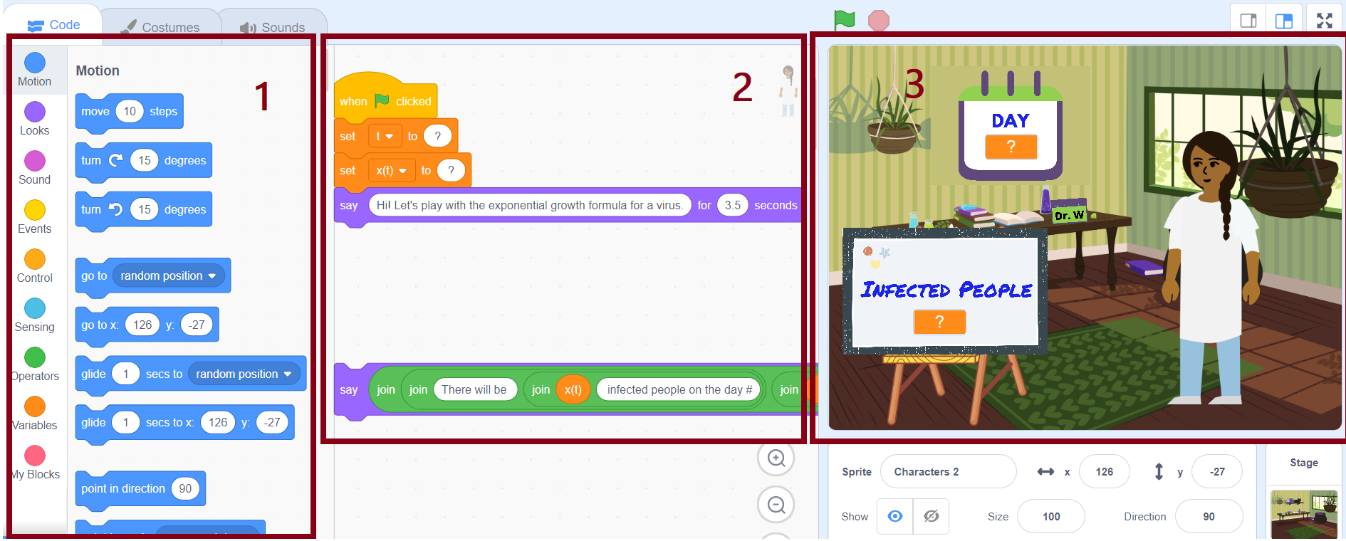
**1.** Open Scratch (<https://scratch.mit.edu/>) and create a free account.

**2.** Follow this link: https://scratch.mit.edu/projects/573368084/editor to open the Exponential Growth project template. **Do not edit this template!**

**3.** **Create a copy** of this template by clicking on *File > Remix*. Work on your new copy (remix) from now on.

**Coding on Scratch**

**1.** Let’s start by familiarizing ourselves with Scratch:



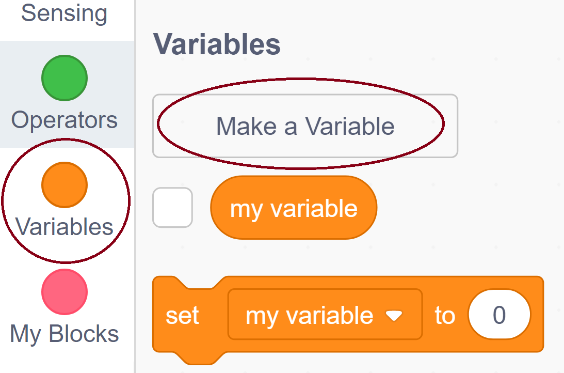
1. The first block (left) contains all the possible lines of code you can use on Scratch. The menu on the far left shows the different categories of code (“Motion”, “Looks”, “Sound”, etc.)
2. The second section (middle) is “your workspace”. This where you write your code by dragging your chosen coding blocks from the first section.

Right now, you should see four lines of code we have pre-written for you. Do you recognize the last line? (Ignore all those “joins”.) What about the first four lines—can you guess what they do?

1. The third block (right) will show the end result of your code.

**2.** Create your variables.

We have created the variables “t” and “xt” for you. Create the variable “b” by clicking on *Variables > Make a Variable.* Create the variable for all sprints.



**3.** Let’s code!

Look at your workspace. We have helped you with the first four lines of code (which are not in your pseudocode) and the last line of code (which is also the last line in your pseudocode). Your job is to fill in the code in between.

To do this, look at all the possible coding blocks listed on the left side on Scratch, and then choose those that most resemble your pseudocode. Work line by line. Part by part. The Scratch translation of your pseudocode should go right after the first three lines of code we have helped you with.

*Hint: Remember that the pseudocode lines in our previous exercises were color-coded. (e.g. “ASK” was turquoise, just as the “Sensing” category on Scratch!)*

**Teachers**

The color-coding from the previous exercises is meant to guide students through the categories on Scratch.

All variables (“xt”, “b”, “t”) were orange, just as the “Variables” category on Scratch. Operators were green, mirroring the green “Operators” category on Scratch.

**Some useful tips:**

* To run and stop the code:

Graphical user interface, application

Description automatically generated with medium confidence

* To add new coding blocks:

Graphical user interface

Description automatically generated

* To use variables and operators:

Graphical user interface, website

Description automatically generated

* To embed blocks:
  + Drag a block towards the container block. Check the highlighted area before dropping it.
* The highlighted area tells you where the block will be placed:

Graphical user interface

Description automatically generated

The new block will be inserted into the first blank space.

A picture containing graphical user interface

Description automatically generated

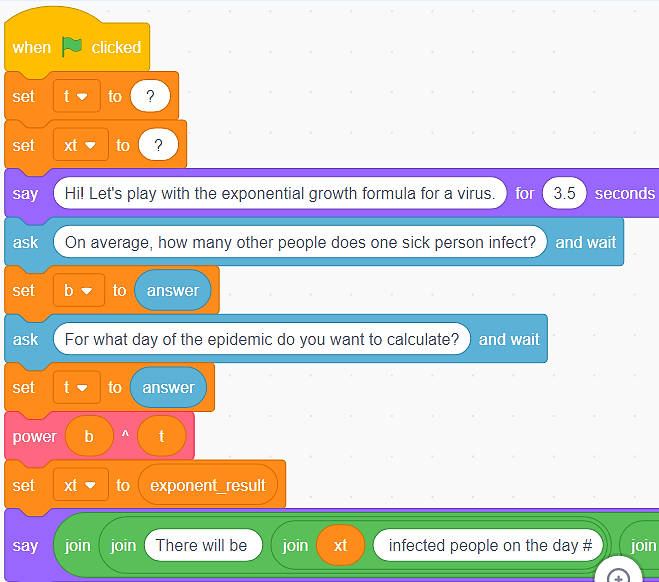
The whole green block will be replaced

Once you finish your code on Scratch, test it! Assume the role of “user” and insert some values. Is the program answering as you intended to? Revise your code if necessary; test it again. Revise it until you get it right.

Happy coding!

**Teachers**

This is what the finished Scratch code looks like:



(The last line is incomplete here due to its length. This line was given to students, however, and they should not modify it.)

You can find the fully functional code here:

<https://scratch.mit.edu/projects/568601710/>

If clicking on the link above does not work, try copying it directly to the address bar.

Tab 4

**Python**

***Matching Pairs Game + Fill in the Blanks***

Match each action of the generalized solution in plain English (left gray column) with its Python equivalent (right gray column). Use the options on the green chart to fill in all the blanks.

***Note: Some of these options will not be used, and some may be used more than once.***

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| Choose from the following options to fill in the blanks: | | | | | | |
|  |  |  |  |  |  |  |
| does one sick person infect |  | bt |  | x0 |  | For what day of the epidemic do you want to calculate? |
|  |  |  |  |  |  |  |
| b |  | xt |  | answer |  | t |

**Not all options in the right gray column will be used.**

|  |  |  |
| --- | --- | --- |
| **Solution Process**  **For Python** |  | **Pseudocode** |
| **1.** Ask: “On average, how many other people  **does one sick person infect** ?” and store whatever the user *inputs* in a variable called “b”. Additionally, specify that “b” will be an integer\* number. |  | b = int(input("On average, how many people  **does one sick person infect** ?")) |
|  |  | b = (input("On average, how many people \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_  \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_?")) |
| **2.** Ask: “**For what day of the epidemic do you want to calculate?**” and store whatever the user *inputs* in a variable called “t”. Additionally, specify that “t” will be an integer\* number. |  | print ("There will be", **xt**, "infected people on the day #", **t**, "of the epidemic.") |
|  |  | t = intg(answer("\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_  \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_?")) |
|  |  | b = int(input("\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_  \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_?")) |
| **3.** Calculate “b^t” and save the result of the calculation in a variable called “xt”. |  | t = int(input("**For what day of the epidemic do you want to calculate?**?")) |
| **4.** Print on screen a message that says how many infected people (xt) there will be at the time (t) that the user has chosen. |  | xt = pow(b, t) |

*\*Hint: The program does not know whether the user’s input will be text (which cannot be used for mathematical operations) or numbers (which can be used for mathematical operations). Thus, you need to specify what type of input (text, integers, decimals) the program should expect.*

***Reorder the Code***

Now that you have matched each step with its Python equivalent, write the whole Python code below in the right order:

b = int(input("On average, how many people does one sick person infect ?"))

t = int(input("For what day of the epidemic do you want to calculate??"))

xt = pow(b, t)

print ("There will be", xt, "infected people on the day #", t, "of the epidemic.")

***Run Your Code***

**1.** Open Jupyter Notebook: <https://jupyter.org/try>

**2.** Open JupyterLab and wait a few seconds for it to load.

**3.** Click on “Python 3” under “Notebook”.

**4.** Type the Python code you wrote above into your workspace.

Graphical user interface, application, Word

Description automatically generated

**5.** Click on the Play button to run your code and test it. If necessary, revise the code until you get it right.

**6.** Congratulations! You just coded the Exponential Growth Formula in Python.

**Teachers**

**Here are some common typing errors in case you need to troubleshoot:**

* **Forgetting** a comma, parenthesis, or some other **punctuation mark**.
* **Order of characters.** (e.g. Misplacing a comma inside of the quotation marks when it should be outside, or vice versa.)
* **Mismatched quotation marks.** (e.g. Combining single with double quotation marks, or straight with curved quotation marks.)
* **Inconsistent capitalization of variables.** (e.g. Naming a variable “Mini” but then trying to use it as “mini”.)

**Note:** Remind students that these are, not silly, but rather common mistakes even within the coding community. Even the most proficient coder can spend hours debugging his faulty program only to find that he had forgotten a comma!

References

[1] Wikipedia Contributors, “Western African Ebola Virus Epidemic,” *Wikipedia*, 12-Dec-2021. [Online]. Available: https://en.wikipedia.org/wiki/Western\_African\_Ebola\_virus\_epidemic. [Accessed: 15-Dec-2021].

[2] M. Grandjean, “Connected world: Untangling the Air Traffic Network,” *Martin Grandjean*, May-2016. [Online]. Available: http://www.martingrandjean.ch/connected-world-air-traffic-network/. [Accessed: 15-Dec-2021].

[3] WHO Ebola Response Team, “After Ebola in West Africa — Unpredictable Risks, Preventable Epidemics,” New England Journal of Medicine, vol. 375, no. 6, pp. 587–596, 2016. [Online]. Available: https://www.who.int/ebola/publications/nejm-after-ebola.pdf. [Accessed: 15-Dec-2021].

1. [2] http://www.martingrandjean.ch/wp-content/uploads/2016/05/airports-map-small.png [↑](#footnote-ref-1)
2. Trust us. This will be important later. [↑](#footnote-ref-2)